Abstract

Support vector machines (SVMs) are a set of related supervised learning algorithm developed by vladimir vapnik in the mid 90's for classification and regression. It is a new generation learning algorithms based on recent advances in statistical learning theory, and applied to large number of real-world applications, such as text categorization and hand-written character recognition. The elegance and the rigorous mathematical foundations from optimization and statistical learning theory have propelled SVMs to the very forefront of the machine learning field within the last decade.

In this paper we will see a method for applying SVM learning algorism for data classification and regression purpose.
1. Introduction

Support Vector Machines, are supervised learning machines based on statistical learning theory that can be used for pattern recognition and regression. Statistical learning theory can identify rather precisely the factors that need to be taken into account to learn successfully certain simple types of algorithms, however, real-world applications usually need more complex models and algorithms (such as neural networks), that makes them much harder to analyse theoretically. SVMs can be seen as lying at the intersection of learning theory and practice. They construct models that are complex enough (containing a large class of neural networks for instance) and yet that are simple enough to be analysed mathematically. This is because an SVM can be seen as a linear algorithm in a high-dimensional space.

In this document, we will primarily concentrate on Support Vector Machines as used in pattern Recognition and function approximation. In the first section we will introduce pattern recognition and hyperplane classifiers, simple linear machines on which SVMs are based. We will then proceed to see how SVMs are able to go beyond the limitations of linear learning machines by introducing the kernel function, which paves the way to find a nonlinear decision function, in this section we will see different kind of kernels and parameter selection. Finally, we will see regression.
2. Pattern Recognition and Hyperplane Classifiers

In pattern recognition we are given training data of the form

\[(x_1, y_1), \ldots, (x_m, y_m) \in \mathbb{R}^n \times \{-1, 1\},\]

that is n-dimensional patterns (vectors) \(x_i\) and their labels \(y_i\). A label with the value of +1 denotes that the vector is classified to class +1 and a label of −1 denotes that the vector is part of class −1. We thus try to find a function \(f(x) = y : \mathbb{R}^n \rightarrow \{+1, -1\}\) that apart from correctly classifying the patterns in the training data (a relatively simple task), correctly classifies unseen patterns too. This is called generalisation.

It is imperative that we restrict the class of functions that our machine can learn, otherwise learning the underlying function is impossible. It is for this reason that SVMs are based on the class of hyperplanes

\[w \cdot x + b = 0, \quad w \in \mathbb{R}^n, \quad b \in \mathbb{R}\]

Where the vector \(w\) defines a direction perpendicular to a hyperplane while varying the value of \(b\) move the hyperplane parallel to itself (figure 1). Which basically divide the input space into two: one part containing vectors of the class −1 and the other containing those that are part of class +1 (see Figure 1). If there exists such a hyperplane, the data is said to be linearly separable. To find the class of a particular vector \(x\), we use the following decision function

\[f(x) = \text{sign}(w \cdot x + b)\]

![Figure 1. A separating hyperplanes \((w, b)\) for a two dimensional(2D) training set.](image-url)
2.1 The Optimal Hyperplane

As we can see from the right hand side of figure 1, there are more than one hyperplane that correctly classifies the training examples. So the question is which of the linear separator is optimal and how can we get this optimal separator?

As you can see from figure 2 below, it has been shown that the hyperplane that guarantees the best generalisation performance is the one with the maximal margin of separation between the two classes \( \frac{2}{\|w\|} \). This type of hyperplane is known as the optimal or maximal margin hyperplane and is unique.

![Support vectors](image)

**Fig. 2. A maximal margin hyperplane with its support vectors**

To calculate the margin, two parallel hyperplanes are constructed, one on each side of the separating hyperplane (figure 2), which are "pushed up against" the two data sets. Intuitively, a good separation is achieved by the hyperplane that has the largest distance to the neighboring datapoints of both classes, since in general the larger the margin the better the generalization error of the classifier.

Assume we are given a set of \( S \) of point of \( x_i \in \mathbb{R}^n \) with \( i=1,2,3...m \). each point \( x_i \) belongs to either of two classes and thus given a level \( y_i \in \{-1,1\} \). The goal is to establish the equation of hyperplane which separates the positive from the negative examples (a “separating hyperplane”) while maximizing the minimum distance between either of the two classes and the hyperplane. For the linearly separable case, the support vector algorithm simply looks for the separating hyperplane with largest margin. This can be formulated as follows:

\[
\begin{align*}
\mathbf{w}.x_i + b &\geq 1 \quad \text{for } y_i = 1 \\
\mathbf{w}.x_i + b &\leq -1 \quad \text{for } y_i = -1
\end{align*}
\]

These can be combined into one set of inequalities:
\( y_i(w \cdot x_i + b) - 1 \geq 0 \quad \forall i \) (2)

the pair \((w, b)\) define a hyperplane of equation
\[
    w \cdot x + b = 0
\]

named separating hyperplane. The quantity \(\frac{2}{||w||}\) which measures the distance between the two class in the direction of \(w\) is called margin.

\(\frac{1}{||w||}\) is the lower bound the distance between the point \(x_i\) and the separating hyperplane \((w, x_i)\).

So given a linearly separable set \(S\), the optimal separable hyperplane is the separating hyperplane which maximize the distance of the closee point of \(S\).

Since the distance of the closest point equals to \(\frac{1}{||w||}\) the optimal separable hyperplane can be regards as the solution of the problem of maximizing subjected to constraints (2), i.e.

\[
    \text{Mimimizing } \frac{||w||^2}{2}
\]

Subjected to:
\[
    y_i(w \cdot x_i + b) - 1 \geq 0
\]

Thus we can find the pair of hyperplanes which gives the maximum margin by minimizing \(||w||^2\) subject to constraints (2). Thus we expect the solution for a typical two dimensional case to have the form shown in Figure 2. Those training points for which the equality in Eq. (2) holds (i.e. those which wind up lying on one of the hyperplanes \(w \cdot x + b = 1\) or \(w \cdot x + b = -1\)), and whose removal would change the solution found, are called support vectors; they are indicated in Figure 2.

The above constraint problem can be solved by using method of lagrangian multipliers. There are two reasons for doing this. The first is that the constraints in (2) will be replaced by constraints on the Lagrange multipliers themselves, which will be much easier to handle. The second is that in this reformulation of the problem, the training data will only appear (in the actual training and test algorithms) in the form of dot products between vectors. This is a crucial property which will allow us to generalize the procedure to the nonlinear case.

Thus, we introduce positive Lagrange multipliers \(\alpha_i\), \(i=1,2,...,m\), one for each of the inequality constraints (2). Recall that the rule is that for constraints of the form \(c_i \geq 0\), the constraint equations are multiplied by positive Lagrange multipliers and subtracted from the objective function, to form the Lagrangian. For equality constraints, the Lagrange multipliers are unconstrained. This gives Lagrangian:

\[
    L = \frac{1}{2}||w||^2 - \sum_{i=1}^{m} \alpha_i y_i(x_i \cdot w + b) + \sum_{i=1}^{m} \alpha_i
\] (3)
Now this is a convex quadratic programming problem, so the solution of the problem is equivalent to determining the saddle points of the above lagrangian.

\[
\frac{\partial L}{\partial b} = \sum_{i=1}^{m} y_ia_i = 0 \quad (4)
\]

\[
\frac{\partial L}{\partial w} = w \cdot \sum_{i=1}^{m} a_ii_i = 0
\]

\[
W = \sum_{i=1}^{m} a_ii_i \quad (5)
\]

If we substitute equation (4) and (5) into equation 3, we get

\[
L(\alpha) = \sum_{i=1}^{m} \alpha_i - \frac{1}{2} \sum_{i,j}^{m} \alpha_i \alpha_j y_iy_jx_i.x_j \quad (6)
\]

The new problem is called dual formulation of our first primal problem (equation 3). It has the property that the maximum of \(L\), subject to constraints \(\alpha \geq 0\), occurs at the same values of \(w, b\) and \(\alpha\), as the minimum of \(L\), subjected to constraints

\[
y_i( w.x_i + b ) - 1 \geq 0.
\]

so we can formulated the dual problem as

Maximizing \(L(\alpha) = \sum_{i=1}^{m} \alpha_i - \frac{1}{2} \sum_{i,j}^{m} \alpha_i \alpha_j y_iy_jx_i.x_j\)

Subjected to \(\sum_{i=1}^{m} y_ia_i = 0\)

\(\alpha \geq 0\)

Note that the only \(\alpha_i\) that can be non zero in equation (6) are those for which the constraints in (2) are satisfied with equality sign. The corresponding point \(x_i\), termed support vectors, are the points of \(S\) closes to the optimal separate hyperplane see figure 3 for geometrical interpretation.

So given the parameter \(w\), the parameter \(b\) can be obtain as:

\[b = y_i - w.x_i\]

Therefore, the problem of classifying a new data point \(x\) is now simply solved by computing

\[\text{sign}(\sum_{i=1}^{m} a_ii_i.x + b)\]

where \(x_i\) is support vector.
As we saw till now basic linear learning machines are only suitable for linearly separable problems. But real world applications often require a more expressive hypothesis space than linear functions can provide.

So how can we manage if the two classes are contain like outlier, noise or some kind of error and can not be separated by linear classifier? In the following section we will give answer for this question.

2.2 Soft Margin Classifier

If the training set not linearly separable, the standard approach is to allow the fat decision margin to make a few mistakes (some points - outliers or noisy examples - are inside or on the wrong side of the margin) see figure 4.
We then pay a cost for each misclassified example, which depends on how far it is from meeting the margin requirement given in Equation (2). To implement this, we introduce *slack variables* $\xi_i$. *Slack variables* $\xi_i$ can be added to allow misclassification of difficult or noisy examples, resulting margin called *soft margin*.

A non-zero value for all $\xi_i$ allows $x_i$ to not meet the margin requirement at a cost proportional to the value of $\xi_i$. So the condition for the optimal hyper-plane (equation 2) can be relaxed by including $\xi_i$:

$$y_i (w . x_i + b) \geq 1 - \xi_i$$  \hspace{1cm} (7)

if the point $x_i$ satisfies inequality to (2) then $\xi_i$ is zero and the above equation reduce to equation (2). Instead if $x$ does not satisfy inequality in equation (2), the term $\xi_i$ is subtract from the right side of 2 to obtain the equation (7). The generalized OSH(optimal separable hyperplane) is regards as the solution to:

$$\text{minimizing} \frac{1}{2} \|w\|^2 + C\sum_{i=1}^{m} \xi_i$$  \hspace{1cm} (8)

subjected to $y_i (w . x_i + b) \geq 1 - \xi_i$

$$\xi \geq 0$$

The term $\sum_{i=1}^{m} \xi_i$ can be thought of as some measure of amount of misclassificication. In other word the term $\sum_{i=1}^{m} \xi_i$ makes the OSH less sensitive to the presence of outliers in the training set. Here $C$ is a regularization parameter that controls the trade-off between maximizing the margin and minimizing the training error. Small $C$ tends to emphasize the margin while ignoring the outliers in the training data, while large $C$ may tend to overfit the training data.

If we follow similar steps As We did for linear separable case we can see the dual problem is identical to separable case. And its Lagrangian Dual Problem formulation is:

$$\text{Maximizing} L(\alpha) = \sum_{i=1}^{m} \alpha_i - \frac{1}{2} \sum_{i,j}^{m} \alpha_i \alpha_j y_i y_j x_i . x_j$$

Subjected to:

$$\sum_{i=1}^{m} y_i \alpha_i = 0$$

$$0 \leq \alpha_i \leq C$$

This is very similar to the optimization problem in the linear separable case, except that there is an upper bound $C$ on $\alpha_i$ now.
2.3. Nonlinear kernels

Till now we saw data sets that are linearly separable(with some noise) . But what are we going to do if the datasets are to hard to separate linearly?

Linear learning machines (such as the hyperplane classifier) have limited computational power and thus limited real-world value. In general, complex real-world applications require a learning machine with much more expressive power.

In most cases real world problems produce datasets which are hard to do linear separtion in inpute space. Fortunatly ,we can extend the linear sepration theory to nonlinear separating surfaces by mapping the input points into feature points and looking for the OSH in the crosponding future space (cortes and vapnik 1995).

If $x \in \mathbb{R}^n$ is an input point ,we let $\phi(x)$ be the corresponding feature point with $\phi$ a mapping from $\mathbb{R}^n$ to certain space $Z$ called feature space . Clearly ,an OSH in $Z$ corresponds a nonlinear separating surafce in inpute space (figure 5).

Figure 5 projecting data that is not linearly separable into a higher dimensional space can make it linearly separable

We have alraedy notice in previous section in SVM formulation ,the training data only appear in the form of the dot products $x_i x_j$ i.e. the optimal hyperplane classifier uses only dot products between vectors in input space. And the same is true in the decision function. In feature space this will translate to $\phi(x_i) \cdot \phi(x_j)$.

$\Phi: \mathbb{R}^n \rightarrow Z$

Clearly, this is very computationally expensive, especially if the mapping is to a high-dimensional space.But many litrature show as kernel function can be used to accomplish the same result in a very simple and efficient way.

A kernel is a function $k(x, x_i)$ that given two vectors in input space, returns the dot product of their images in feature space.
K(x_i, x_j)= \phi(x_i) \cdot \phi(x_j) \tag{9}

So by computing the dot product directly using a kernel function, one avoid the mapping \phi(x). This is desirable because Z has possibly infinite dimensions and \phi(x) can be tricky or impossible to compute. Using a kernel function, one need not explicitly know what \phi(x) is. By using a kernel function, a SVM that operates in infinite dimensional space can be constructed. And the decision function will be:

\[ f(x) = \sum_{i=1}^{m} a_i y_i K(x_i, x_j) + b \tag{10} \]

Where for every new test data, the kernel function for each SV need to be recomputed. And a kernel function K is such a function that corresponds to a dot product in some expanded feature space.

But what kind of kernel function is used? i.e. is there any constraint on the type of kernel function suitable for this task. For any kernel function suitable for SVM, there must exist at least one pair of \{Z, \phi\}, such that Eqn.(9) is true, i.e. the kernel function represents the dot product of the data in Z.

There are several different kernels, choosing one depends on the task at hand. The commonly used family of kernels are the following:

**Polynomial kernel**

\[ K(x_i, x_j) = (1 + x_i \cdot x_j)^d \]

results in a classifier that is a polynomial of degree \(p = 2, 3,...\) in the data. And \(p\) is user defined parameter.

The polynomial kernel function is directional, i.e. the output depends on the direction of the two vectors in low-dimensional space. This is due to the dot product in the kernel. All vectors with the same direction will have a high output from the kernel. The magnitude of the output is also dependent on the magnitude of the vector \(x_i\).

**Radial basis kernel**

Commonly used radial basis kernel is gaussian kernel:

\[ K(x_i, x_j) = \exp\left(-\frac{||x_i-x_j||^2}{2\sigma^2}\right) \]

Gives a Gaussian radial basis function classifier. The output of the kernel is dependent on the Euclidean distance of \(x_j\) from \(x_i\) (one of these will be the support vector and the other will be the testing data point). The support vector will be the centre of the RBF and \(\sigma\) will determine the area of influence this support vector has over the data space and it is user defined parameter. Larger value of \(\sigma\) will give a smoother decision surface and more regular decision boundary. This is because an RBF with large \(\sigma\) will allow a support vector to have a
strong influence over a larger area. A larger $\sigma$-value will also reduce the number of support vectors. Since each support vector can cover a larger space, fewer are needed to define a boundary.

**Sigmoid kernel:**

$$K(x, y) = \tanh(\kappa x^T y + \theta)$$

With user defined parameter $\kappa$ and $\theta$.

It is originated from neural networks and it has similar features like MLP.

Note: It does not satisfy equation (9) for all $\kappa$ and $\theta$ values.

**Example:**

Let's see how $\phi$ looks like for polynomial features.

Take polynomial kernel with $p=2$ and

Let's input be two dimensional vector $x=[x_1 \ x_2]$;

i.e. $K(x_i, x_j) = (1 + x_i^T x_j)^2$,

Need to show that $K(x_i, x_j) = \phi(x_i)^T \phi(x_j)$:

$$K(x_i, x_j) = (1 + x_i^T x_j)^2,$$

$$= 1 + x_i^T x_j + 2 x_i x_j + x_i^T x_j + 2 x_i x_j + 2 x_i x_j = [1 \ x_i^2 \ \sqrt{2} x_i x_j \ x_j^2 \ \sqrt{2} x_i x_j \ x_j^2 \ \sqrt{2} x_i x_j \ x_j^2]$$

$$= \phi(x_i)^T \phi(x_j), \ \text{where} \ \phi(x) = [1 \ x_1^2 \ \sqrt{2} x_1 x_2 \ x_2^2 \ \sqrt{2} x_1 \ \sqrt{2} x_2]$$

2.4. Parameter Selection

SVM has only two major parameters which are defined by the user. There is the trade-off between the margin width and the classification error ($C$), and the kernel function. Most kernel functions will also have a set of parameters. The trade-off between maximum margin and the classification error (during training) is defined by the value $C$ in Eqn. (8). The value $C$ is called the Error Penalty. A high error penalty will force the SVM training to avoid classification errors. A larger $C$ will result in a larger search space for the QP optimizer. This generally increases the duration of the QP search. Other experiments with larger numbers of data points (1200) fail to converge when $C$ is set higher than 1000. This is mainly due to numerical problems.
Selecting a specific kernel and parameters is usually done in a try-and-see manner. The following simple procedures help us to select these parameters:

1. Conduct simple scaling on the data
2. Consider RBF kernel, \( K(x_i, x_j) = \exp\left(-\frac{||x_i-x_j||^2}{2\sigma^2}\right) \)
3. Use cross-validation to find the best parameter \( C \) and \( \sigma \)
4. Use the best \( C \) and \( \sigma \) to train the whole training set
5. Test

And we can summarize SVM algorithm as follows:

1. Choose a kernel function
2. Choose a value for \( C \)
3. Solve the quadratic programming problem (many software packages available)
4. Construct the discriminant function from the support vectors

Generally we can summarize what we saw till now by using the graph below.
3. Support vector Machine Regression (SVR)

Support Vector method can also be applied to the case of regression, maintaining all the main features that characterize the maximal margin algorithm. The model produced by support vector classification (as described above) only depends on a subset of the training data, because the cost function for building the model does not care about training points that lie beyond the margin. Analogously, the model produced by SVR only depends on a subset of the training data, because the cost function for building the model ignores any training data that are close (within a threshold $\varepsilon$) to the model prediction (see figure 7).

The regression problem can be stated as:

Suppose we are given training data $\{(x_i, y_i) \mid i=1, 2, \ldots, m\}$, of input vectors $x_i$ associated targets $y_i$, and the goal is to fit a function $f(x)$ which approximates the relation inherited between the data set points and it can be used later on to infer the output $y_i$ for a new input data point $x$. Any practical regression algorithm has a loss function $L(y, f(x))$, which describes how the estimated function deviated from the true one. Many forms for the loss function can be found in the literature. In this tutorial, Vapnik's loss function is used, which is known as $\varepsilon$- insensitive loss function and defined as:

$$L(y, f(x)) = \begin{cases} 
0 & \text{if } |y - f(x)| \leq \varepsilon \\
(y - f(x)) - \varepsilon & \text{otherwise}
\end{cases}$$

Figure 6 linear and non linear regressions with epsilon intensive band

Where $\varepsilon > 0$ is a predefined constant which controls the noise tolerance. With the $\varepsilon$-insensitive loss function, the goal is to find $f(x)$ that has at most $\varepsilon$ deviation from the actually obtained targets $y_i$ for all training data. In other words, the regression algorithm does not care about errors as long as they are less than $\varepsilon$, but will not accept any deviation larger than this. In the same way as with classification approach there is motivation to seek and optimize the
generalization bounds given for regression. They relied on defining the loss function that ignores errors, which are situated within the certain distance of the true value. This type of function is often called – epsilon intensive – loss function. Figure (6) above shows an example of linear and non linear regression function with – epsilon intensive – band. The variables measure the cost of the errors on the training points. These are zero for all points that are inside the band, figure (7).

Figure 7 the soft margin loss setting correspondins for linear svm

One of the most important ideas in Support Vector Classification and Regression cases is that presenting the solution by means of small subset of training points gives enormous computational advantages. Using the epsilon intensive loss function we ensure existence of the global minimum and at the same time optimization of reliable generalization bound. In general, SVM classification and regression are performed using a nonlinear kernel $K(x_i, x_j)$.

For simplicity of notation, Let see the case of linear functions $f$, taking the form

$$f(x) = \mathbf{w} \cdot \mathbf{x} + b$$

the regression problem can be written as a convex optimization problem:

$${\text{minimize}} \; \frac{1}{2} \| \mathbf{w} \|^2$$

subjected to $\quad y_i \cdot (\mathbf{w} \cdot \mathbf{x}_i + b) \leq \varepsilon$  \hspace{1cm} (12)

$$+ (\mathbf{w} \cdot \mathbf{x}_i + b) - y_i \leq \varepsilon$$

The assumption in (12) was that such a function $f$ actually exist that approximates all pairs $(x,y)$ with $\varepsilon$ precision, or in other words, that the convex optimization problem is feasible. Sometimes however, this may not be the case, or we also may want to allow for some errors.
Analogously to the soft margin loss function, one can introduce slack variables $\xi_i, \xi_i^*$ to cope with, otherwise infeasible constraints of the optimization problem (12). So our optimization problem becomes:

Minimize $\frac{1}{2} \|w\|^2 + C \sum_{i=1}^{m} (\xi_i + \xi_i^*)$

Subject to $y_i - (w \cdot x_i + b) \leq \varepsilon + \xi_i$  

$(w \cdot x_i + b) - y_i \leq \varepsilon + \xi_i^*$  

$\xi_i, \xi_i^* \geq 0$  

The constant $C > 0$ determines the trade off between the flatness of $f$ and the amount up to which deviations larger than $\varepsilon$ are tolerated.

As shown in Fig. 7, only the points outside the shaded region contribute to the cost insofar as the deviations are penalized in a linear fashion. It turns out that in most cases the optimization problem Eq. (13) can be solved more easily in its dual formulation. Moreover, the dual formulation provides the key for extending SVM machine to nonlinear functions. Hence, a standard dualization method utilizing Lagrange multipliers will be described as follows.

$L = \frac{1}{2} \|w\|^2 + C \sum_{i=1}^{m} (\xi_i + \xi_i^*) - \sum_{i=1}^{m} \alpha_i (\varepsilon + \xi_i - y_i + w \cdot x_i + b) - \sum_{i=1}^{m} \alpha_i^* (\varepsilon + \xi_i^* + y_i - w \cdot x_i + b) - \sum_{i=1}^{m} (\lambda_i \xi_i + \lambda_i^* \xi_i^*)$  

Here $L$ is the Lagrangian and $\alpha_i, \alpha_i^*, \lambda_i, \lambda_i^*$ are Lagrange multipliers. Hence the dual variables in Eq. (7) have to satisfy positivity constraints:

$\alpha_i, \alpha_i^*, \lambda_i, \lambda_i^* \geq 0$  

It follows from the saddle point condition that the partial derivatives of $L$ with respect to the primal variables $(w, b, \xi_i, \xi_i^*)$ have to vanish for optimality. And if we follow similar steps like what we did for classification optimization problem above we end up with the dual optimization problem. By deriving the dual problem we already eliminated the dual variables $\lambda_i, \lambda_i^*$. Thus

$f(x) = \sum_{i=1}^{m} (\alpha_i - \alpha_i^*)(x_i \cdot x_j) + b$  

Note that the complete algorithm can be described in terms of dot products between the data. Even when evaluating $f(x)$ we need not compute $w$ explicitly. These observations will come in handy for the formulation of a nonlinear extension. For new given $x$ the corresponding value given by:

$f(x) = \sum_{i=1}^{m} (\alpha_i^* - \alpha_i) K(x_i, x) + b$
Only data for which \( \alpha_i \neq \alpha_i^* \) contribute. This occurs only if
\[
|f(x_i) - y_i| \geq \epsilon \quad \text{(outside tube)}
\]

4. SVM Vs Neural network

A Support Vector Machine (SVM) performs classification by constructing an \( N \)-dimensional hyperplane that optimally separates the data into two categories. SVM models are closely related to neural networks. In fact, a SVM model using a sigmoid kernel function is equivalent to a two-layer, perceptron neural network.

Support Vector Machine (SVM) models are a close to classical multilayer perceptron neural networks. Using a kernel function, SVM’s are an alternative training method for polynomial, radial basis function and multi-layer perceptron classifiers in which the weights of the network are found by solving a quadratic programming problem with linear constraints, rather than by solving a non-convex, unconstrained minimization problem as in standard neural network training. Generally we can characterized the two as follows.

**Neural network**
- Universal approximation of continuous nonlinear functions
- Learning from input-output patterns; either off-line or on-line learning
- Parallel network architecture, multiple inputs and outputs
- Feedforward and recurrent networks
- Supervised and unsupervised learning applications

**Problems:**
- Existence of many local minima!
- How many neurons and layers needed for a given task?

**Support Vector Machine**
- Learning involves optimization of a convex function (no false minima, unlike a neural network)

Nonlinear classification and function estimation by convex optimization
with a unique solution and primal-dual interpretations.

- Number of neurons (support vectors) automatically follows from a convex program.
- Learning and generalization in huge dimensional input spaces (able to avoid the curse of dimensionality!).
- Use of kernels (e.g. linear, polynomial, RBF...)

**Problem:** SVM formulation does not include criteria to select kernel function that give good generalization. So getting kernel function and parameters are some how trial and error.
5. Summary

Support Vector Machines have been applied to many real-world problems, producing state of the art results. These include text categorisation, image classification, and handwritten character recognition.

SVMs provide a new approach to the problem of pattern recognition (together with regression estimation and linear operator inversion) with clear connections to the underlying statistical learning theory. They differ radically from comparable approaches such as neural networks: SVM training always finds a global minimum, and their simple geometric interpretation provides fertile ground for further investigation. An SVM is largely characterized by the choice of its kernel, and SVMs thus link the problems they are designed for with a large body of existing work on kernel based methods.

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